

Tune-scans and working point optimization for colliding beams in HL-LHC

Dobrin Kaltchev (Triumf)

and

D. Pellegrini, N. Karastathis, Y. Papaphilippou (CERN)

(in conjunction with their talks at this meeting)

with the help of

Riccardo de Maria, E. McIntosh, A. Mereghetti (CERN)

CERN-TRIUMF HL-LHC collaboration

Outline

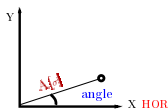
- 1 Tune-scan (TS) Procedure
- 2 Domains
- 3 1D (Linear) TS
- 4 Resonances new: 16th order
- 5 2D TS
- 6 New working point – a “candidate” for future studies

Tune-scan procedure: MadX+SixTrack environment

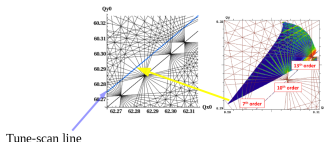
HL-LHC lattice
 V1.2, V1.3
 collision settings

Beam-Beam + sextupoles +
 <octupoles> (HL-LHC)

Initial coordinates:
 amplitude $\mathbf{A}[\sigma]$ and
 real-space **angle**



Note: SixTrack adjusts
 tunes with beam-beam ON,
 i.e. “sharp edge” $Q_{x,y}^{BB}$:
 $Q_{x,y}^{BB} = Q_{x,y}^0 - \Delta Q_{x,y}^{BB}$



Nominal HL-LHC
 footprint at 2.2 E11

Tune-scan procedure: MadX+SixTrack env.

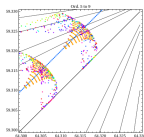
Output from Six-Track OCT. = lattice octupoles

want to place footprint on the res. mesh

NO
OCT.

some SixTrack footprints:
1-12 σ ; 10^4 turns; **tune=1**

(here hue prop. to slope of dist. betw twins)



Tune-scan procedure: MadX+SixTrack env.

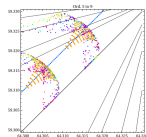
Output from Six-Track OCT. = lattice octupoles

want to place footprint on the res. mesh

NO
OCT.

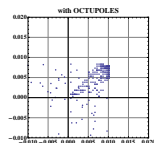
some SixTrack footprints:
1-12 σ ; 10^4 turns; **tune=1**

(here hue prop. to slope of dist. betw twins)



WITH
OCT.

reduced size in direction \perp
diagonal



Tune-scan procedure: MadX+SixTrack env.

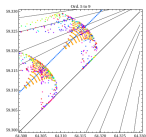
Output from Six-Track OCT. = lattice octupoles

want to place footprint on the res. mesh

NO
OCT.

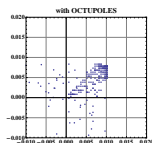
some SixTrack footprints:
1-12 σ ; 10^4 turns; **tune=1**

(here hue prop. to slope of dist. betw twins)

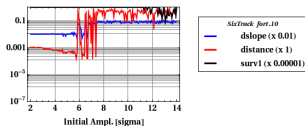


WITH
OCT.

reduced size in direction \perp
diagonal



- 1) survival turns for 2 twins
- 2) distance between twins
- 3) slope of dist. etc



Tune-scan procedure: MadX+SixTrack env.

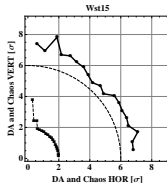
Output from Six-Track (LONG term) 10^6 turns BOINC or HTCondor

dynamic apert. (DA)
 = last surv part. =
 = Min[surv1,surv2]

also chaotic border,
 but not reported here

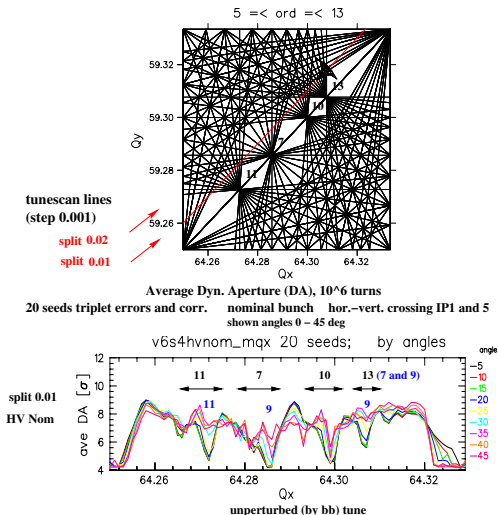
Tune-scans (TS):

1D TS: DA-by-angle dep. on tune
2D TS: MIN DA over 20 angles dep. on tune



Old (<2010) studies – LHC

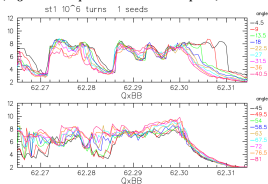
along Line || diag., +0.01, OCT=0, low chrom.=2
 losses =dips mostly in HOR. plane max. res. ord. = 13



Tune-scan procedure: HL-LHC Steps

1) Contour DA-by-angle. 2) Extend in 2D. 3) add octupoles + high. chr.

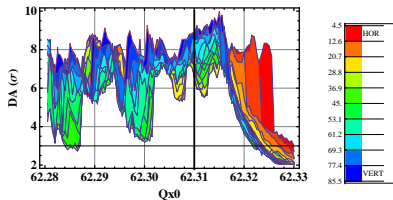
HL-LHC old-style plot: DA [sigma] by initial angle
(angle=0 means part. launched in HOR plane)



old style plot
< 2010

18 azimuthal angles
split into two plots

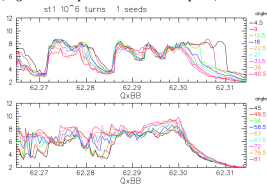
New-style "DA by angle" with contours



Tune-scan procedure: HL-LHC Steps

1) Contour DA-by-angle. 2) Extend in 2D. 3) add octupoles + high. chr.

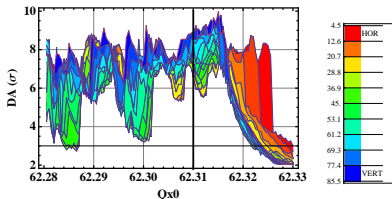
HL-LHC old-style plot: DA [sigma] by initial angle
(angle=0 means part. launched in HOR plane)



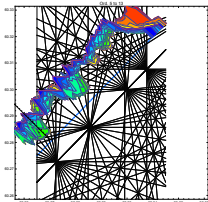
old style plot
< 2010

18 azimuthal
angles
split into two plots

New-style "DA by angle" with contours

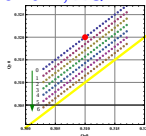


Correlate DA Maxima and Dips
with Resonances



Extend in 2D towards diag. (yellow)

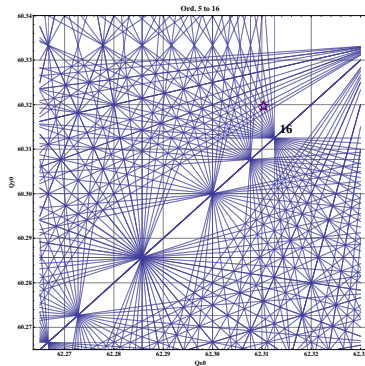
$$\Delta Q^{\parallel \text{diag.}} \geq 5 \cdot 10^{-4}, \Delta Q^{\perp \text{diag.}} \geq \sqrt{2} \cdot 10^{-3}$$



Tune-scan procedure: Domains

resonances 5-16 ord

clusters right to left: **16**,13,10,7+14,11



Tune-scan procedure: Domains

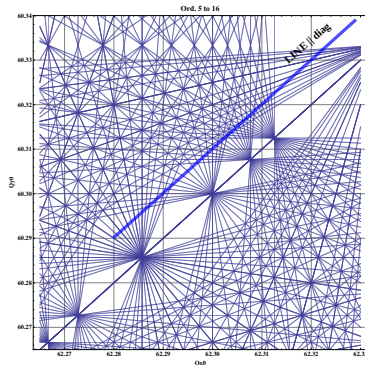
resonances 5-16 ord

clusters right to left: **16**,13,10,7+14,11

1) Linear TS (no oct)

along +0.01 line: $\Delta Q_{\parallel} = 5 \cdot 10^{-4}$

HL-LHC V1.2 and LHC



Tune-scan procedure: Domains

resonances 5-16 ord

clusters right to left: **16**,13,10,7+14,11

1) Linear TS (no oct)

along +0.01 line: $\Delta Q^{\parallel} = 5 \cdot 10^{-4}$

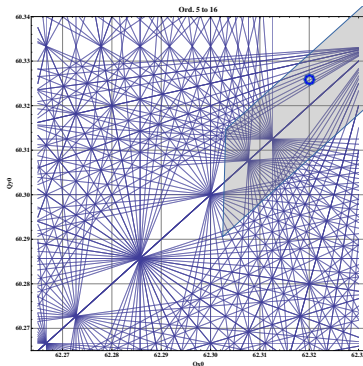
HL-LHC V1.2 and LHC

2) 2D (oct., chr=15) near 1/3

base-line WP (Yannis,Dario,Nikos)

HL-LHC V1.2 and V1.3

$\Delta Q^{\parallel} = 2 \cdot 10^{-3}$, $\Delta Q^{\perp} = 2.3 \cdot 10^{-3}$



Tune-scan procedure: Domains

resonances 5-16 ord

clusters right to left: **16,13,10,7+14,11**

1) Linear TS (no oct)

along +0.01 line: $\Delta Q^{\parallel} = 5 \cdot 10^{-4}$

HL-LHC V1.2 and LHC

2) 2D (oct., chr=15) near 1/3

base-line WP (Yannis,Dario,Nikos)

HL-LHC V1.2 and V1.3

$\Delta Q^{\parallel} = 2 \cdot 10^{-3}, \Delta Q^{\perp} = 2.3 \cdot 10^{-3}$

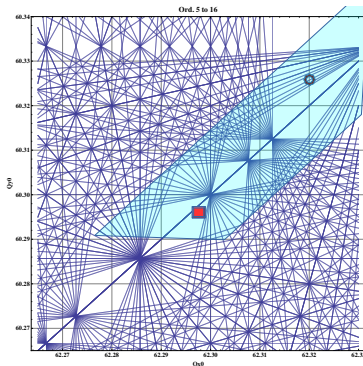
3) 2D (oct., chr=15) extended

with params at end of level.

new candidate WP near 10th ord cl.

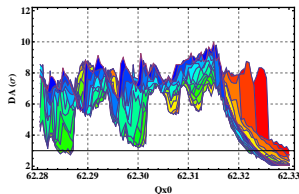
HL-LHC V1.3

$\Delta Q^{\parallel} = 5 \cdot 10^{-4}, \Delta Q^{\perp} = 2.8 \cdot 10^{-3}$

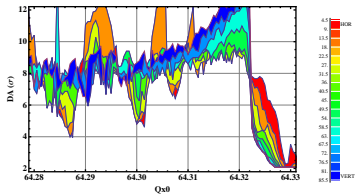


Linear TS (no oct) : DA by-angle “HL-LHC case 0”

HL-LHC BB + Sext $N_b = 1.1 \cdot 10^{11}$



LHC as-built BB + Sext + corr. tripl. err. seed 1



Shown contours of constant dynamic aperture with color hue proportional to the angle (angle=0 part. launched in HOR plane) every second angle plotted

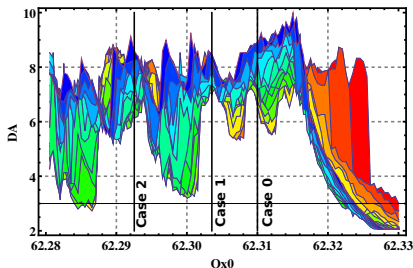
HL-LHC parameters (call this case 0):

- HLLHCv1.2; intensity: 1.1×10^{11} ; single HO replaces full crabs chr=3
- IR1,5 Xing half-ang = $295 \mu\text{rad}$, $\beta^* = 15 \text{ cm}$
- IR8 $\beta^* = 1 \text{ m}$, Xing half-ang = $-135+250=-115 \mu\text{rad}$ (LHCb spect. pol.=+1)
- IR2 $\beta^* = 10 \text{ m}$, hor. sep., Xing = $170 \mu\text{rad}$
- emit_n = $2.5 \mu\text{m}$, bunch length = 7.5 cm , $\frac{\Delta p}{p} = 2.7 \times 10^{-4}$, bunch spacing 25 ns, chrom=3

HL-LHC cases with $\Delta Q_x^{BB} \sim 0.02$ and 0.03

are predicted to be already at optimum

Vert. axis is only valid for **case 0**.



case	comment	tune shift	Qx0
0	as scan made $N_b = 1.1 \cdot 10^{11}$	0.0155	62.31
1	$N_b = 2.2 \cdot 10^{11}$, no BB in IP8	0.022	62.3035
2	$N_b = 2.2 \cdot 10^{11}$, with BB in IP8	0.033	62.2925

E.g. for Case 1: the predicted $Qx0 = 62.31 - (0.022 - 0.0155) = 62.3035$.

It is seen to be *exactly* at optimum loc.!

“Delta-function” head (footprint shape → symmetries)

Linear TS (no oct) :

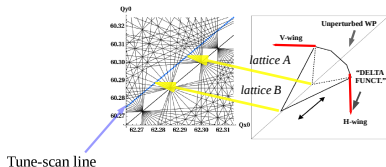
If only interested in optimum loc., then one scan is enough.

A TS made with setup A **can predict** optimum tunes for setup B of different ΔQ_x^{BB} since the head scans the **same resonances** at a distance = difference between the tune-shifts of B and A.

- 1) losses occur mostly near the high- σ head
- 2) head's projection on the hor. axis is very close to unperturbed tune point

naive table: octupoles OFF ($H \leftrightarrow V$)

DA-loss in setup A	Active point on H plane	escape dir	TS transl. symmetry
H plane	H wing	V	H



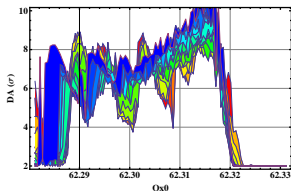
Linear TS (no oct) – HOR plane dominates – H-wing scans resonances as “ δ – function” 1D model is enough to predict dips

Check the prediction

Perform TS with true setups of cases 1 and 2.

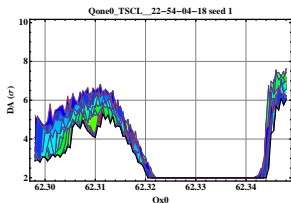
Min DA contours near 62.31 should (locally) look the same as on slide 10, and they do

case 1 $N_b = 2.2 \cdot 10^{11}$ BB in IR2,8 ON, CC ON (full), $\beta_{IP8}^* = 3\text{m}$ with neg. polarity, Hirata ON.



CHECK: .31 falls at optimum

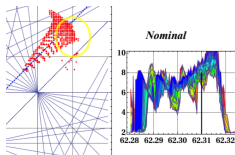
case 2 $N_b = 2.2 \cdot 10^{11}$ ($\Delta Q_x^{BB} = 0.033$).



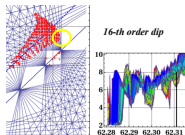
CHECK: .31 falls near optimum (+ 0.002)

Linear TS (no oct) – HL-LHC Footprint Slider

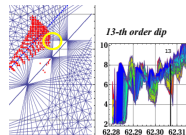
Near nominal WP one sees 16th ord (neglected before). Valid for LHC too, only DA scaled.



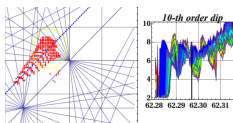
(a) HOR, 16th order



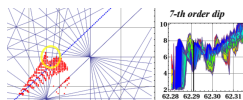
(b) HOR, 16th order



(c) HOR, 13th order



(d) HOR+VERT, 10th ord



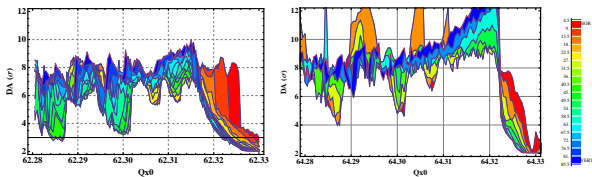
(e) VERT, 7(14) ord

For plots on the right, vert. black line shows Q_x^0 .

Animations: t1 t2 t3 local: t1 t2 t3

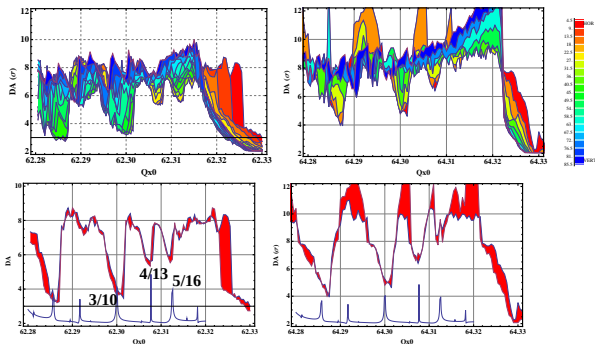
Linear TS (no oct) Resonance dips via distorted ellipse

3 or 2-IP HO Lie (CS) invariant in H plane agrees (wherever HOR plane dominates) Left: HL-LHC, 1.1×10^{11} ; Right: LHC as-built:



Linear TS (no oct) Resonance dips via distorted ellipse

3 or 2-IP HO Lie (CS) invariant in H plane agrees (wherever HOR plane dominates) Left: HL-LHC, 1.1×10^{11} ; Right: LHC as-built:

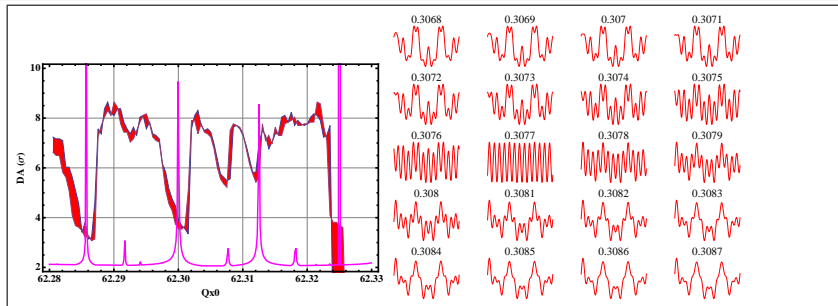


Bottom two: **Red** curve – only near HOR plane.

Blue peaks: high-order-harmonic amplitude of the **1D** Lie-inv.

The 4/13 peak depends on $\Delta \nu_{IP5-IP1}$ (=0 for $0.25 \times$ integer).

Two Head-On IPs Lie (Courant-Sn.) invariant continued



- Magenta (left) = $\text{Max}_{n=1}^{n=40}$, red curves (right) = $\sum_{n=1}^{n=40}$ of:

$$\frac{2 n c_n(A)}{\sin(n \mu_x / 2)} \cos [n(\phi + \mu_x / 2 + \Delta \mu_{51} / 2)] \cos (n \Delta \mu_{51} / 2)$$

$c_n(A)$ = res coef (dr. terms), $A=10 \sigma_x$, $\mu_x \equiv 2\pi Qx_0$, $\Delta \mu_{51} \equiv 2\pi \Delta \nu_{IP5-IP1}$,

$\phi = 0.1(\text{arb.})$, $\Delta \nu_{IP5-IP1}=31.2104$

- Same finding: of 2 peaks near nominal 62.31, the 4/13 depends on $\Delta \nu_{IP5-IP1}$, the one above nom. does not.

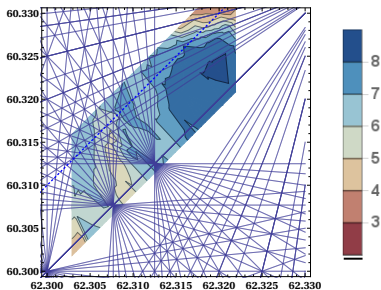
Summary of Linear TS (no oct) along line || diag

- **HL-LHC lattices w/o octupoles are already at optimum tunes for (these three) more-important scenarios (and for LHC)**
- **The role of 16-th ord resonances in HOR plane near nom WP (no octupoles, chr ~ 3)**
- **Need of 2D Tune-scans (HL-LHC, with octupoles, chr = 15)**

2D TS (Min DA of 20 ang); near 1/3

still $Q' = 3$, $I_{MO}=0$, $\beta^*=15$ cm stays constant (NOT a leveling scenario)

$$1) N_b = 1.1 \times 10^{11}$$



- HL-LHC V1.2
- fraction_crab=1
- IR1,5 Xing half-ang = 295 μ rad

2D TS (Min DA of 20 ang); near 1/3

still $Q' = 3$, $I_{MO}=0$, $\beta^*=15$ cm stays constant (NOT a leveling scenario)

$$1) N_b = 1.1 \times 10^{11}$$

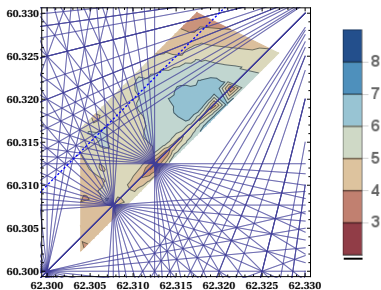
$$2) N_b = 2.2 \times 10^{11}$$

shift of opt WP = VERT

no oct.

DA $\sim 6\sigma$

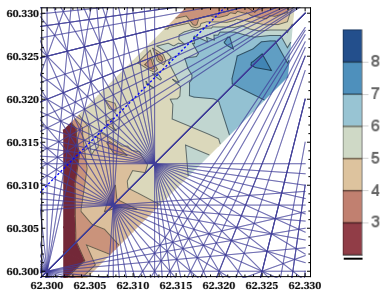
- HL-LHC V1.2
- fraction_crab=1
- IR1,5 Xing half-ang = 295 μ rad



2D TS (Min DA of 20 ang); near 1/3

now with $Q' = 15$, $I_{MO} = -570$, $\beta^* = 20$ cm stays constant (NOT a leveling scenario)

$$1) N_b = 1.1 \times 10^{11}$$



- HL-LHC V1.2
- fraction_crab=.75
- IR1,5 Xing half-ang = 295 μ rad

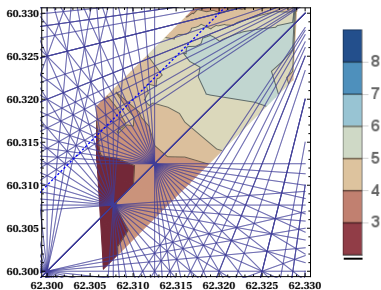
2D TS (Min DA of 20 ang); near 1/3

now with $Q' = 15$, $I_{MO} = -570$, $\beta^* = 20$ cm stays constant (NOT a leveling scenario)

$$1) N_b = 1.1 \times 10^{11}$$

$$2) N_b = 2.2 \times 10^{11}$$

shift of opt WP = || diag
(octupoles)

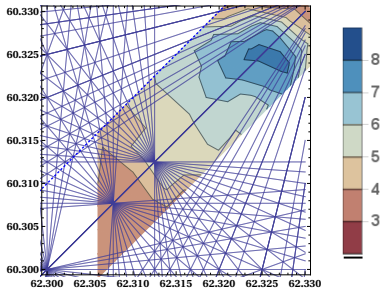


- HL-LHC V1.2
- fraction_crab=.75
- IR1,5 Xing half-ang = 295 μ rad

2D TS (Min DA of 20 ang); near 1/3

$Q' = 15, I_{MO} = -570$ Beg. and End of leveling

Beg: $\beta^* = 46\text{cm}, N_b = 2.2 \cdot 10^{11}$



- HL-LHC V1.3 fraction_crab=0.75 (190)
- IR1,5 Xing half-ang = 250 μrad
- IR8 $\beta^* = 3\text{m}$, Xing half-ang = $-135+250=-115 \mu\text{rad}$
- IR2 $\beta^* = 10\text{m}$, hor. sep., Xing = 240 μrad

2D TS (Min DA of 20 ang); near 1/3

$Q' = 15, I_{MO} = -570$ Beg. and End of leveling

Beg: $\beta^* = 46\text{cm}, N_b = 2.2 \cdot 10^{11}$

End: $\beta^* = 15\text{cm}, N_b = 1.2 \cdot 10^{11}$

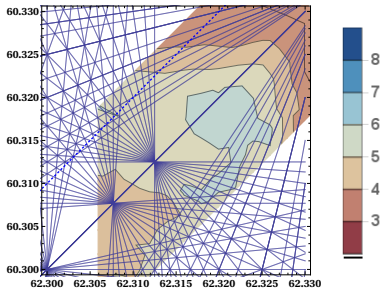
shift || diag.

agrees with N. Karastathis:

Beg: (62.32, 60.325)

End: (62.315, 60.32)

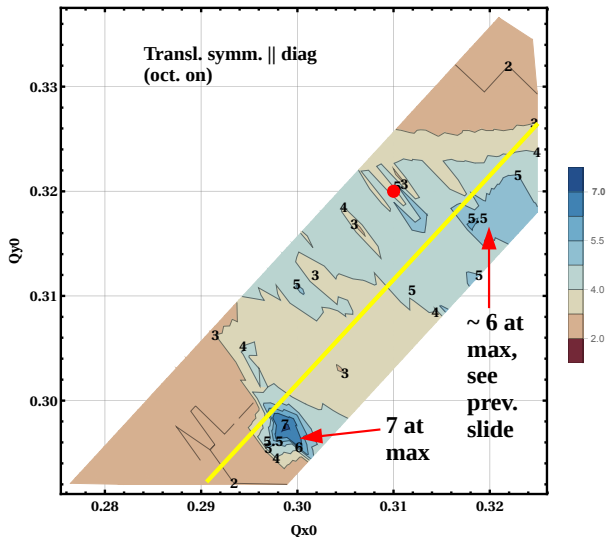
(for $I_{MO} = -300$)



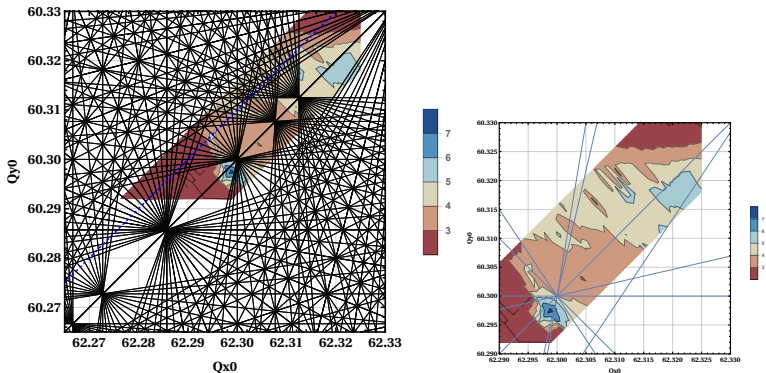
- HL-LHC V1.3 fraction_crab=0.75 (190)
- IR1,5 Xing half-ang = 250 μrad
- IR8 $\beta^* = 3\text{m}$, Xing half-ang = $-135+250 = -115 \mu\text{rad}$
- IR2 $\beta^* = 10\text{m}$, hor. sep., Xing = 240 μrad

2D TS, End Fill, Min DA 20 ang new WP candidate

Near 10th order res. cluster; Higher maximum by 1 – 1.5 σ , but good region smaller



2D TS (Min DA, 20 ang) – a new WP candidate



Left: Resonances of orders from 5 to 16 and the new possibly interesting region near the 10th-order res. cluster. **Right:** some resonance lines nearby:

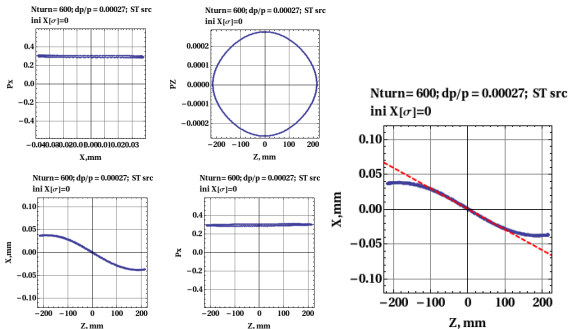
$$\begin{aligned}
 Q_x - Q_y &= 2 & 9Q_x - 6Q_y &= 199 \\
 13Q_x - 3Q_y &= 629 & 10Q_y &= 603 \\
 12Q_x - 2Q_y &= 627 & 6Q_x + 4Q_y &= 615 \\
 2Q_x - 12Q_y &= 627 & 5Q_x + 5Q_y &= 613 \\
 3Q_x - 13Q_y &= -597 & &
 \end{aligned}$$

Thank You

spare slides

SixTrack test: Crab Cav. in IP5 and IR1

want to see rotated bunch



ST tracking for about one synchr. oscillation: phase spaces at IP5 of HL-LHC for Xing ang=295, CC=ON, BB=ON with CO added. Plots remain the same if IP5 \rightarrow IP1, changing also the axes $X \rightarrow Y$, $PX \rightarrow PY$. Red dashed line on the right plot shows the action of an ideal CC kick; $X_{ini} = 0$, $Y_{ini}=0$.

SixTrack Test: Hirata kicks

for BB ON in IR1,5 and 8 (look as expected)

Top: X and Y (m) after each of the 5 slices in IP5, 8 and 1, at the first turn of a particle starting at zero betatron amplitude. It has momentum offset 0.00027.

Bottom: accumulated PX and PY (rad) after each slice.

